

# EC114 - INTRODUCTION TO QUANTITATIVE ECONOMICS

## TEST: SOLUTIONS

23-11-2006

### Question 1

1.  $Pr(C \text{ or } S) = Pr(C) + Pr(S) - Pr(C \text{ and } S) = 0.80 + 0.60 - 0.50 = 0.90$
2.  $Pr(H \text{ and } 3) = Pr(H) \times Pr(3) = 1/2 * 1/6 = 1/12$
3. Letting  $L = \text{lemon}$ ,  $Pr(L) = 0.10$ ;  $Pr(\text{sale}|L) = 0.90$ ;  $Pr(\text{sale}|non-L) = 0.05$ .  
Bayes' rule gives:

$$Pr(L|\text{sale}) = \frac{Pr(L) \times Pr(\text{sale}|L)}{Pr(L) \times Pr(\text{sale}|L) + Pr(non-L) \times Pr(\text{sale}|non-L)} = \frac{0.10 * 0.90}{0.10 * 0.90 + 0.90 * 0.05} = 2/3$$

### Question 2

In each case, we calculate the hit probability  $P$  such that:

$$0 = (\text{profit if a hit})(P) + (\text{profit if a dud})(1-P)$$

which implies:

$$P = \frac{-(\text{profit if a dud})}{(\text{profit if a hit}) - (\text{profit if a dud})}$$

The answers are:

Dick Tracy	$\pounds 47 / \pounds 158 = 0.297$
Die Hard II	$\pounds 69 / \pounds 152 = 0.454$
Total Recall	$\pounds 16 / \pounds 118 = 0.136$

Die Hard II has the highest requisite probability; Total Recall has the lowest requisite probability.

### Question 3

1.  $Pr(X < 1) = Pr(Z < \frac{1-3}{1}) = Pr(Z < -2) = 0.0228$
2.  $Pr(X > 5) = Pr(Z > \frac{5-3}{1}) = Pr(Z > 2) = 0.0228$
3. The expected value of the cost per machine is  $0.0228(\pounds 250) = \pounds 5.70$ , and Whirl-away would have to add this to the price of each machine to cover the cost of the guarantee.

### Question 4

The mean of this sample of 24 observations is:

$$\frac{112+120+\dots+110}{24} = 111.875$$

The standard deviation of  $X$  is assumed to be 8, which implies a standard deviation for the sample mean of  $\frac{8}{\sqrt{24}}$ .

1. A 95% confidence interval is  $111.875 \pm 1.96(8/\sqrt{24}) = 111.875 \pm 3.20$ .
2. A 99% confidence interval is  $111.875 \pm 2.58(8/\sqrt{24}) = 111.875 \pm 4.21$ .
3. The 99% confidence interval is wider because we have to include more possibilities to be more certain that the interval will encompass the true value of  $\mu$ .
4. Generally, the width of a 95% confidence interval  $\bar{X} \pm 1.96\sigma/\sqrt{n}$  is  $2(1.96)\sigma/\sqrt{n}$ . To halve this interval, we must double the square root of  $n$ , which requires a quadrupling of  $n$ , the sample size.