

UNIVERSITY OF ESSEX

AUTUMN MID-TERM TEST, THURSDAY 24 NOVEMBER 2011

INTRODUCTION TO QUANTITATIVE ECONOMICS

Time allowed: 60 minutes.

Write your name, your registration number, your class teacher's name, and your class number clearly on the front page of your answer book(s).

Candidates must answer ALL questions.

This paper consists of THREE questions.

This paper carries 99 marks in total. To arrive at a score out of 100, you will be given 1 mark extra.

A statistical table can be found on page 4.

Candidates are allowed to bring into the examination room:
calculators (hand held, containing no textual information).

Please do not leave your seat unless you are given permission by an invigilator.

Do not communicate in any way with any other candidate in the examination room.

Do not open the question paper until told to do so.

All answers must be written in the answer book(s) provided.

All rough work must be written in the answer book(s) provided. A line should be drawn through any rough work to indicate to the examiner that it is not part of the work to be marked.

At the end of the examination, remain seated until your answer book(s) have been collected and you have been told you may leave.

Question 1

We randomly sample the exam scores (out of 20) of 7 students:

10, 12, 7, 8, 14, 3, 15

- a) (12 marks) Define and calculate the sample mean and median score.
- b) (12 marks) Define and calculate the sample variance, standard deviation and mean absolute deviation of the scores.
- c) (9 marks) We are interested in the underlying population parameters. Define and calculate an unbiased estimator of the population variance. Very briefly suggest an unbiased estimator of the median (we have not covered this in lectures - I am looking for a sensible and reasoned answer).

Question 2

Among the population of EC114 students, the probability of being from the UK is 0.7. The probability of preferring micro-economics to macro-economics is 0.6. The probability of preferring macro to micro is 0.4 (i.e. nobody is indifferent between the two). The probability of both being from the UK and preferring micro is 0.42.

- a) (10 marks) Draw these events in a Venn diagram.
- b) (10 marks) What is the probability of either being from the UK or preferring micro?
- c) (6 marks) Are the events “being from the UK” and “preferring micro” independent or not? Why?
- d) (7 marks) What is the probability of preferring macro given that you are NOT from the UK?

Question 3

The probability of winning on a particular fruit machine is independent across time. I play the fruit machine 100 times. I only care about my number of successes, not about how much I win. To model the chance of success, I decide to apply the central limit theorem and use a normal approximation. I am told that the mean number of successes is 20 and the variance is 16.

- a) (12 marks) Draw a graph of the approximate distribution of successes, marking on the horizontal axis the mean and one standard deviation either side of the mean.

- b) (14 marks) What is the probability of getting between 15 and 22 successes?
- c) (7 marks) I realize I can compute exact probabilities. Why is this? What is the chance of getting exactly 0 successes?

(END OF PAPER)

Areas under the standard normal curve

z'	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.0000	0.0040	0.0080	0.0120	0.0160	0.0199	0.0239	0.0279	0.0319	0.0359
0.1	0.0398	0.0438	0.0478	0.0517	0.0557	0.0596	0.0636	0.0675	0.0714	0.0753
0.2	0.0793	0.0832	0.0871	0.0910	0.0948	0.0987	0.1026	0.1064	0.1103	0.1141
0.3	0.1179	0.1217	0.1255	0.1293	0.1331	0.1368	0.1406	0.1443	0.1480	0.1517
0.4	0.1554	0.1591	0.1628	0.1664	0.1700	0.1736	0.1772	0.1808	0.1844	0.1879
0.5	0.1915	0.1950	0.1985	0.2019	0.2054	0.2088	0.2123	0.2157	0.2190	0.2224
0.6	0.2257	0.2291	0.2324	0.2357	0.2389	0.2422	0.2454	0.2486	0.2517	0.2549
0.7	0.2580	0.2611	0.2642	0.2673	0.2704	0.2734	0.2764	0.2794	0.2823	0.2852
0.8	0.2881	0.2910	0.2939	0.2967	0.2995	0.3023	0.3051	0.3078	0.3106	0.3133
0.9	0.3159	0.3186	0.3212	0.3238	0.3264	0.3289	0.3315	0.3340	0.3365	0.3389
1.0	0.3413	0.3438	0.3461	0.3485	0.3508	0.3531	0.3554	0.3577	0.3599	0.3621
1.1	0.3643	0.3665	0.3686	0.3708	0.3729	0.3749	0.3770	0.3790	0.3810	0.3830
1.2	0.3849	0.3869	0.3888	0.3907	0.3925	0.3944	0.3962	0.3980	0.3997	0.4015
1.3	0.4032	0.4049	0.4066	0.4082	0.4099	0.4115	0.4131	0.4147	0.4162	0.4177
1.4	0.4192	0.4207	0.4222	0.4236	0.4251	0.4265	0.4279	0.4292	0.4306	0.4319
1.5	0.4332	0.4345	0.4357	0.4370	0.4382	0.4394	0.4406	0.4418	0.4429	0.4441
1.6	0.4452	0.4463	0.4474	0.4484	0.4495	0.4505	0.4515	0.4525	0.4535	0.4545
1.7	0.4554	0.4564	0.4573	0.4582	0.4591	0.4599	0.4608	0.4616	0.4625	0.4633
1.8	0.4641	0.4649	0.4656	0.4664	0.4671	0.4678	0.4686	0.4693	0.4699	0.4706
1.9	0.4713	0.4719	0.4726	0.4732	0.4738	0.4744	0.4750	0.4756	0.4761	0.4767
2.0	0.4772	0.4778	0.4783	0.4788	0.4793	0.4798	0.4803	0.4808	0.4812	0.4817
2.1	0.4821	0.4826	0.4830	0.4834	0.4838	0.4842	0.4846	0.4850	0.4854	0.4857
2.2	0.4861	0.4864	0.4868	0.4871	0.4875	0.4878	0.4881	0.4884	0.4887	0.4890
2.3	0.4893	0.4896	0.4898	0.4901	0.4904	0.4906	0.4909	0.4911	0.4913	0.4916
2.4	0.4918	0.4920	0.4922	0.4925	0.4927	0.4929	0.4931	0.4932	0.4934	0.4936
2.5	0.4938	0.4940	0.4941	0.4943	0.4945	0.4946	0.4948	0.4949	0.4951	0.4952
2.6	0.4953	0.4955	0.4956	0.4957	0.4959	0.4960	0.4961	0.4962	0.4963	0.4964
2.7	0.4965	0.4966	0.4967	0.4968	0.4969	0.4970	0.4971	0.4972	0.4973	0.4974
2.8	0.4974	0.4975	0.4976	0.4977	0.4977	0.4978	0.4979	0.4979	0.4980	0.4981
2.9	0.4981	0.4982	0.4982	0.4983	0.4984	0.4984	0.4985	0.4985	0.4986	0.4986
3.0	0.4987	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990