

# Trade with Incomplete information: “The Lemons Problem”

Based on Akerlof (1970)

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 $x \sim U(0, 1)$  (standard uniform distribution; go over this)

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Note: An equilibrium profile must specify a complete strategy for Buyer, i.e., a function  $B^*(p) \in \{0, 1\}$ . It is wlog to assume that such a strategy will be “Buy if  $p \leq \bar{p}$ ” for some maximum price  $\bar{p}$ .

## Payoffs:

Buyer values the car at  $\frac{3}{2}x$ ;

thus gets payoff  $u_B = \begin{cases} \frac{3}{2}x - p & \text{if buy} \\ 0 & \text{otherwise} \end{cases}$  (we assume separable utility here)

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**Efficient outcome:** Buyer must buy the car.

Any price  $p$  s.t.  $x \leq p \leq \frac{3}{2}x$  will yield trade and will be a Pareto-improvement over no trade.

## Equilibrium outcome:

Buyer's equilibrium strategy must set  $\bar{p} = \frac{3}{2}E(x|p)$ . I.e., buy if the price is below  $\frac{3}{2}$  of buyer's expectation over the quality of the car – where that expectation will depend on the price offered!

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What does this mean? For any price  $p$  offered, the Buyer values the product at  $\frac{3}{4}p$ . Thus, for any price offered, the Buyer will reject! Thus, the only equilibrium must involve no trade, and thus be inefficient!

Any profile  $\{p(x) = \text{whatever}; \text{reject always}\}$  (paired with certain beliefs ... see next week) is an equilibrium.

We can allow  $\{p(x) = \text{whatever}, p(0) = 0; \text{accept only if } p = 0\}$  ,  
but who cares?

Note: See Watson's "Jerry and Freddy" for a simpler example.